Spatial Separation of Carrier Spin by the Valley Hall Effect in Monolayer WSe₂ Transistors

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Supporting Information

ABSTRACT: We investigate the valley Hall effect (VHE) in monolayer WSe₂ field-effect transistors using optical Kerr rotation measurements at 20 K. While studies of the VHE have so far focused on n-doped MoS₂, we observe the VHE in WSe₂ in both the n- and p-doping regimes. Hole doping enables access to the large spin-splitting of the valence band of this material. The Kerr rotation measurements probe the spatial distribution of the valley carrier imbalance induced by the VHE. Under current flow, we observe distinct spin-valley polarization along the edges of the transistor channel. From analysis of the magnitude of the Kerr rotation, we infer a spin-valley density of 44 spins/μm, integrated over the edge region in the p-doped regime. Assuming a spin diffusion length less than 0.1 μm, this corresponds to a spin-valley polarization of the holes exceeding 1%.

KEYWORDS: Tungsten diselenide, magneto-optical Kerr effect, valleytronics, spintronics

Ultra-thin semiconducting transition metal dichalcogenides (TMDCs) have attracted attention for next-generation nanoelectronics because of their highly tunable optical and electronic properties.¹⁻⁴ They also have potential for spin- and valleytronics. In particular, with strong spin–orbit coupling and broken inversion symmetry at monolayer thickness, these materials are expected to exhibit a coupled spin and valley Hall effect (VHE).⁵⁻⁷ The monolayer TMDCs feature nonzero Berry curvature, combined with a large (hundreds of meV) spin splitting, ΔSOC-⊥ in the valence band and smaller spin splitting, ΔSOC-∥ in the conduction band at the K and K’ band extrema (Figure 1a). The Berry curvature and spin of carriers in the valence and conduction bands around the K and K’ points are equal in magnitude but opposite in sign.⁵⁻⁷ In addition to its fundamental interest, the VHE in TMDCs could lead to novel device applications, such as an electrically gate-controlled method to switch nanomagnets for spintronics and memory.

Previous work has demonstrated the VHE in monolayer and bilayer n-doped MoS₂⁵,⁸ through the observation of the spatial separation of carriers in the K and K’ valleys under current flow in the semiconductor. The present work complements these earlier studies by exploring the phenomenon in monolayer WSe₂ in both the n- and p-doped regimes. In WSe₂, both the valence and conduction band spin splitting are significant, 460 and 30 meV, respectively.⁹⁻¹¹ Thus, in our low-temperature measurements, the VHE carries spin along with the valley information for both electrons and holes. Because of the large spin splitting of the valence band, we expect that holes in a given valley retain their spin information even at room temperature. Thus, p-type TMDCs including WSe₂ are promising candidates for spin-based applications at elevated temperatures. The large spin splitting also makes the VHE for holes more resistant to influence of magnetic fields and Rashba-related contributions to the Berry phase.¹²,¹³

For this work, we fabricated WSe₂ field-effect transistors (FETs) to measure the accumulation of valley and spin polarized carriers under different gating and bias conditions. Figure 1b,c illustrates, respectively, the transistor structure and the influence of the VHE when current flows through the channel. We control the transistor through its source-drain voltage VDS (with source voltage as reference), which creates an in-plane electric field Eř and charge (sheet) current density Jř along the channel, and a back-gate voltage VGS, which modulates the Fermi level in the WSe₂ channel. For appropriate bias voltages VDS and VGS, a spin-valley Hall current Jř is generated perpendicular to the charge current across the sample. Note that no external magnetic field needs to be applied.

Optical Characterization of Valley Hall Effect. We probe the presence of valley- and spin- polarized carriers using the valley circular dichroism of the monolayer WSe₂ through...
measurement of optical Kerr rotation (see Supporting Information Section S1 for measurement details). As shown in Figure 1a, light of σ+ (σ−) circular polarization selectively probes transitions in the K (K′) valley. Thus, if the valley carrier populations are different, the dielectric function for the two circularly polarized states of light will also differ. Correspondingly, linearly polarized light will acquire a Kerr rotation (KR) angle, θKR, in passing through or being reflected from the sample supported on a substrate.

An optical image of the device is shown in Figure 1d. We map the effect of the VHE by recording the KR with a tightly focused laser while rastering the sample in the transverse (x̂) direction. The sample was supported on SiO2 (100 nm) on a highly doped Si substrate, which served as our back-gate (see Supporting Information Section S2 for details about the device). We used gate voltages VGS = −30 or 30 V with a sinusoidally varying drain voltage of VDS = 5 V (peak voltage, in Volts) at frequencies from 200 to 800 Hz and detected synchronously the electric signal from the Kerr rotation measurement with a lock-in amplifier.

The device was studied in a liquid-helium cooled cryostat with a sample temperature confirmed by the peak energy shift in photoluminescence and reflectance measurements. Figure 2a shows the reflection contrast spectrum, ΔR/R0, of the sample at room temperature and at 20 K. The blueshift and narrowing of both the A and B (higher energy) peaks can be seen in the data. In the inset, we fit the A exciton peak in the ΔR/R spectrum, differentiated with respect to photon energy Ei to a dielectric function of the form

$$\epsilon(E) = \epsilon_0 + \sum_i \frac{f_i}{E_{0i} - E^2 - i\gamma_i}$$  (1)

Here f0, E0, and γ are the oscillator strength, resonance energy, and line width of the ith transition, and ε0 is a nonresonant background contribution to the dielectric function. For our device at VGS = 0 V and 20 K, we find that we can describe the A-exciton feature with an oscillator strength of fA = 1.37 eV^2, an energy of E0A = 1.75 eV, and a line width of γA = 28.9 meV. We assume an effective layer thickness of 0.649 nm.

Figure 2b shows ΔR/R spectra as we vary the back-gate voltage. We deduced that our sample is intrinsically n-doped as a higher negative gate-bias is required to observe the positively charged exciton (trion) feature. This asymmetry, arising from unintentional n-doping of the sample, is also reflected in the electrical characteristics of the device presented in Figure 3a,b. The peak around 1.75 eV corresponds to the A exciton resonance and the lower-energy peaks arise from p- and n-doped trions in the highly gated regimes. We fit the reflection contrast derivative for gate voltages of 0 V, −10 V, and −20 V and the resulting parameters for A exciton and p-trion are shown in Figure S2 in Supporting Information Section S3. We use a simple capacitor model, described in the next section, to estimate the associated charge density. If we set the point of charge neutrality to −10 V, we find that the A exciton oscillator strength is reduced by 17% by increasing the gate voltage from −10 V to −20 V. Extrapolating linearly, the exciton absorption should disappear at VGS ≈ −70 V or a charge density of p0 ≈ 10^{13} cm⁻². This behavior agrees with that previously reported for electrons in monolayer WS2 on a SiO2/Si substrate, although a stronger variation of the optical properties with charge density was observed for TMDC monolayers encapsulated in h-BN.

We use the measured doping dependence of the exciton strength to model the expected KR as a function of the valley...
carrier imbalance. For each valley, we assume that the corresponding exciton loses all its oscillator strength for a charge density of \( 5 \times 10^{12} \text{ cm}^{-2} \). Taking into account the relevant optical propagation effects in our device structure, as discussed in the Supporting Information Section S4, we find that the resulting valley imbalance in the valence band per unit Kerr rotation is \( \frac{\Delta \theta}{2 e \mu_{\text{eff}}} = 6.7 \times 10^{-2} \text{ rad} \) for probing at 700 nm, where \( \Delta p = p^\uparrow - p^\downarrow \) is difference in the (sheet) concentrations of spin up and spin down carriers. This conversion factor incorporates contributions from both the real and imaginary parts of the dielectric function of the TMDC layer, which are coupled to polarization rotation of the probe optical field for the multilayered substrate.

In the case of electron doping, we obtained a stronger KR signal on the low-energy side of the A exciton. A KR would result from trion contributions to the optical response,\(^{21-23}\) as discussed in Supporting Information Section S4. We expect that the main contribution at the probe wavelength would be from the lower energy n-type trion.

**Electrical Characterization.** The device current versus gate voltage \( J_D \) characteristics are presented in Figures 3a,b for \( V_{DS} = \pm 3 \) V DC. These data were obtained with approximately the RMS ac voltage applied during the KR measurements, with the same source contact grounded for both the electrical and optical measurements. The reverse bias data (not shown) exhibit weaker current flow. Additional electrical plots are included in Supporting Information Section S5. From these data, we estimate carrier concentrations using a parallel plate capacitor model, \( n = C_{ox}(V_{GS} - V_T)/\epsilon \), where \( n \) is the concentration of electrons or holes, \( \epsilon \) is the elementary charge, \( C_{ox} \approx 34.5 \text{ nF/cm}^2 \) is the oxide capacitance (per unit area), and \( V_T \) is the threshold voltage.\(^{22} \) At \( V_{GS} = -30 \) and 30 V, we found \( n = (2 \pm 1) \times 10^{12} \text{ cm}^{-2} \) in the p-regime and \( n = (3 \pm 1) \times 10^{12} \text{ cm}^{-2} \) in the n-regime, where the error comes from uncertainty in \( V_T \). From the near-linear regime of the \( J_D \) versus \( V_{GS} \) response, we use the transconductance to estimate the field-effect mobility\(^{25} \) of the channel at 20 K. We find mobilities of \( \mu = 0.11 \pm 0.07 \text{ cm}^2/(\text{V s}) \) for the p-regime and \( \mu = 0.81 \pm 0.06 \text{ cm}^2/(\text{V s}) \) for the n-regime. The measured values are 2 orders of magnitude smaller than previous statistical TMDC mobility measurements\(^{26} \) and two or more orders of magnitude smaller than the highest mobilities measured in WSe\(_2\).\(^{27,28} \) The lower apparent mobilities in our samples reflect an underestimate of the true values because of the role of contact resistance in our simple two-terminal measurements. In addition, our devices lack the channel encapsulation typically used to achieve high conductivities.

**Kerr Rotation Scans.** Representative line scans of the KR \( (\theta_K) \) moving across the channel in the transverse \( (\hat{x}) \) direction are shown in Figure 4 for both the p-doped \( (V_{GS} = -30 \) V) and the n-doped \( (V_{GS} = 30 \) V) regimes. On the bare substrate, there is no meaningful KR. We see distinct peaks of \( \theta_K \) of opposite sign on the two sides of the WSe\(_2\) channel. We attribute this effect to the accumulation of carriers with opposite valley (and spin) on the edges of sample as the result of the deflection of the carriers from the VHE. The peaks of \( \theta_K \) are slightly asymmetric. There is a slight offset in the center of the channel, which we ascribe to a magnetoelectric effect associated with unintentional strain in the sample.\(^{29} \)

The measured KR in Figure 4a,b is responsive to the in-plane bias voltage, showing greater \( \theta_K \) for greater \( V_{DS} \) doubling from 3 \( V_p \) to 5 \( V_p \) and disappearing for \( V_{DS} = 0 \) (Figure 4a inset). We have also recorded \( \theta_K \) as a function of \( V_{GS} \) and seen a positive correlation, as discussed in Supporting Information Section S6. The scans for p- and n-doped samples were taken with a 700 nm (1.77 eV) and 730 nm (1.70 eV) laser, respectively. We chose the wavelengths for each doping regime in order to optimize the signal and minimize photodoping induced by the laser. The focused laser spot had a diameter of 1 \( \mu \)m full width at half-maximum (\( \text{fwhm} \)).
Modeling of Results and Discussion. The experimental results of Figure 4a,b show the expected presence of opposite spin-valley polarization at the two edges of the channel. To analyze the results more quantitatively, we consider a spin drift-diffusion model for carrier transport under an applied in-plane electric field $E$. This approach has been used previously to explain the behavior of spin accumulation in GaAs. Because the carrier spin is coupled to valley, we will refer to the carriers with spin-valley characteristics simply as spins in this section.

In steady state, the drift-diffusion model can be solved in closed form for reflecting boundaries and a channel sufficiently wide that the spin accumulation regions on the two edges do not overlap. The spatial distribution of the excess spin density, $s(x)$, across the channel is then given by

$$ s(x) = p^1 - p^2 = \left( S \frac{l_D}{l} \right) \left( e^{-x/w} - e^{-(x-w)/l} \right) $$

where $w$ is the width of the channel, $l_D$ is the spin diffusion length, and $S$ is the integrated spin density (per unit length) along either edge. The parameter $S$ can be written in terms of the spin-lifetime $\tau_s$ as

$$ S = \tau_s \frac{\sigma_l}{\sigma_c} l_D = \tau_s \frac{\sigma_l}{\epsilon} $$

where $\sigma_l$ is the spin-valley Hall conductivity and $\sigma_c$ is the charge (sheet) conductivity. We can approximate the spin diffusion length as $l_D = \sqrt{D\tau_s}$, where $D$ is the carrier diffusivity, which can, in turn, be related to the carrier mobility through the Einstein relationship.

Our experimental KR traces exhibit peaks at the channel edges with width consistent with the Gaussian laser beam profile. This implies that under our experimental conditions $l_D$ is much smaller than the laser spot size.

By integrating the experimental KR profile, we can obtain an estimate of the spin accumulation $S$. In particular, using our inferred value for the relation between intervalley hole density difference and KR, $s_p = 6.7 \times 10^7 \text{cm}^{-2} \mu\text{rad}$, from Figure 4a, we obtain an experimental spin accumulation of $S = 44 \text{mm}^2/\mu\text{m}$ in the p-doped regime. Here we have taken the average of the integrals of the two peaks, subtracting out the uniform background signal present over the sample. To compare $S$ with two-dimensional spin densities, we can write $S = 4.4 \times 10^9 \text{spins/cm}^2\mu\text{m}$, that is, over a width of 1 $\mu$m near the edge of the sample, the average excess spin density is $4.4 \times 10^9 \text{cm}^{-2}$.

Within the drift-diffusion model, we can relate the experimental integrated excess spin obtained to material properties through eq 3. In particular, we make use of our experimental result to estimate the spin lifetime $\tau_s = S \frac{\epsilon}{\sigma_l/\epsilon}$.

To do so, we first determine the current density in our experiment for a dc measurement with $V_{DS} = 3 \text{ V}$ (dc), comparable to our RMS voltage in the KR measurements. We find from Figure 3 a value of $I_x = 10^{-2} \mu\text{A}/\mu\text{m}$, based on the average value of the swept scan of the gate voltage at the relevant gate voltage of $V_{GS} = -30 \text{ V}$. The spin conductivity is taken as $\sigma_l = 1.3 \times 10^{-3} \text{ e}/\hbar$ for $p_0 = 10^{10} \text{ cm}^{-2}$, as predicted by first principle calculations for TMDC monolayers and scaled linearly for the carrier concentration in our sample. Using the hole mobility inferred above from the measured electrical characteristics, we find $\sigma_c = \mu e p_0 = 35 \text{ nS}$. With these parameters, we then obtain $\tau_s = 0.4 \text{ ns}$, a value at the lower end of the range of previously determined spin-polarized hole lifetimes. Since we are likely underestimating $\sigma_c$, we can consider this a lower bound for $\tau_s$.

With an estimate for $\tau_s$ in hand, we can use $l_D = \sqrt{D\tau_s}$ to infer a lower bound for the spin diffusion length of 3 nm. This is consistent with our earlier experimental observation that the diffusion length should be much shorter than the laser spot size (1 $\mu$m). In a pristine sample with mobilities around 100 $\text{cm}^2/\text{V s}$ and valley-polarized lifetimes of 100 ns, we expect diffusion lengths on the order of 1 $\mu$m.

The solid lines in Figure 4a,b show the result of the drift-diffusion model, eq 2, using the experimentally deduced parameters, including a constant offset over the sample and convolution with the 1 $\mu$m fwhm Gaussian laser spatial profile.

Our estimate of the spin diffusion length also allows us to evaluate the degree of spin polarization near the edges. For the lower bound $l_D = 3 \text{ nm}$, we infer approximately 70% spin polarization, $S/\epsilon$, under our experimental conditions. For a longer assumed spin diffusion length of, for example, 100 nm, we would infer from our experimental KR results a spin-valley polarization for holes of 2% at the edge of the sample.

For the n-doped regime, we are also able to fit the peaks in the KR scans to a diffusion length of $l_D < 1 \mu$m. In view of the uncertainties in deducing spin-valley densities from the experimental KR values for the n-doped regime, as discussed above, we have not attempted to analyze quantitatively the magnitude of the measured KR.

In the KR scans for both p- and n-doping, the left peak exhibits a slightly sharper decay than the right peak. We believe that this effect is a scanning artifact, reflecting either a decrease in the channel current after applying a gate bias at the start of the scan or the presence of n-type photodoping as observed in the electrical characteristics and discussed in Supporting Information Sect. S5. In either case, changes should be more significant near the start (left-side) of the scan.

In conclusion, we have investigated the VHE in WSe2 monolayer transistors under current flow for both electron and hole doping by spatially mapping the spin-valley polarization across the channel using the optical Kerr effect. The spatial distribution and magnitude of the spin accumulation agree with a drift-diffusion transport model with reasonable material parameters. In the p-regime, we deduce a spin accumulation of 44 spins/$\mu$m and infer a lower bound of 0.4 ns for the spin lifetime. Because there have been reports of spin lifetimes on the order of 1 $\mu$s, much greater spin accumulations and spin-diffusion lengths should be attainable using improved samples and sample environment. We have shown electrical control of the doping and the spin accumulation from the VHE, and we have observed for the first time the VHE in the p-doped regime. As the valence band spin-splitting greatly exceeds thermal energies at room temperature, studies of the VHE in p-doped samples at higher temperatures are warranted.

### ASSOCIATED CONTENT

#### Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acs.nanolett.8b03838.
Measurement setup, sample fabrication, modeling of reflection contrast, analysis of KR to the valley carrier imbalance, electrical characterization, and the doping dependence of KR.

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Author Contributions
E.B. and J.A.C.-I. conceived and carried out the device fabrication and measurements. S.H.K. built the optical setup and assisted with experiments. C.M. assisted with experiments and analysis. E.P., H.-S.P.W., and T.F.H. supervised the work. All authors contributed to the analysis and interpretation of results and preparation of the manuscript.

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Notes
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